Compactified Horizontal Visibility Graph for the Language Network

D.V. Lande^{1,2}, A.A.Snarskii^{1,2}

¹Institute for information recording, NAS Ukraine, Kiev, Ukraine ²National Technical University "Kiev Polytechnic Institute", Kiev, Ukraine

A compactified horizontal visibility graph for the language network is proposed. It was found that the networks constructed in such way are scale free, and have a property that among the nodes with largest degrees there are words that determine not only a text structure communication, but also its informational structure.

Key words: language network, complex network, scale-free network, visibility graph.

Construction of networks with text elements, words, phrases or fragments of natural language as nodes in some cases allows to detect the structural elements of the text critical for its connected structure and find informationally significant elements, as well as words that are secondary for understanding of the text. Such networks may also be used to identify unconventional text components, such as collocations, supra-phrasal units [1], as well as for finding similar fragments in different texts [2].

There is a multitude of approaches to constructing networks from the texts (so-called language networks) and different ways of interpreting nodes and links, which causes, accordingly, different representation of such networks. Nodes are connected if corresponding words are either adjacent in the text [3, 4], or are in a single sentence [5], or are syntactically [6, 7] or semantically [8, 9] connected.

At the intersection of digital signal processing (DSP) theory and complex network theory there are several ways of constructing networks from the time series, among those are visibility graph construction methods (see survey [10]), namely the horizontal visibility graph (HVG) [11,12]. Based on these approaches, networks can also be constructed from texts in which numeric values are assigned in some manner to each word or phrase. The examples of functions assigning a number to a word are: ordinal number of a unique word in a text, length of the word, "weight" of the word in a text, e.g., generally accepted TFIDF metric (canonically, a product of the term frequency in a text fragment and a binary logarithm of the inverse number of text fragments containing this word – inverse document frequency) or its modifications [13, 14] and other word weight estimates.

In this paper, the standard deviation estimate of word weight is used for constructing word networks [15]. If all the words in the text of N words are numbered in succession (let n=1,...N be the ordinal number of the word in a text, the word position), layout of a certain word A can be designated as $A_k(n)$, where k=1,2,...,K denotes the number of occurrence of this word in a text, and n is a position of this word in a text. For example, $A_3(50)$ means that the third occurrence of the word A has position 50 in the text.

The distance between successive occurrences of the word in these terms would be $\Delta A_k = A_{k+1}(m) - A_k(n) = m - n$, where *m* and *n* are the positions of the *k*+1-th *k*-th occurrences of the word *A* in the text, respectively.

Standard deviation estimate proposed in [15] is calculated as follows:

$$\sigma_{A} = \frac{\sqrt{\left\langle \Delta A^{2} \right\rangle - \left\langle \Delta A \right\rangle^{2}}}{\left\langle \Delta A \right\rangle}, \qquad (1)$$

where $\langle \Delta A \rangle$ is a mean value of the sequence $\Delta A_1, \Delta A_2, ..., \Delta A_K$, $\langle \Delta A^2 \rangle$ is a mean value of $\Delta A_1^2, \Delta A_2^2, ..., \Delta A_K^2$, and *K* is a number of occurrences of the word *A* in the text.

As opposed to other series examined in DSP theory, the series of numerical values assigned to words are transformed into horizontal visibility graphs (HVG), where each node not only has a corresponding numerical value, but also the corresponding word itself.

The process of constructing the language network using HVG consists of two stages. At the first stage, the traditional HVG is constructed [16]. To do that a series of nodes is put on the horizontal axis, where each node corresponds to a word in order of occurrence in the text, and standard deviation estimates are put on the vertical axis (visually a histogram, see fig. 1). There is a connection between nodes if they are in "line of sight" with each other, i.e., if they can be connected by a horizontal line that does not cross any other histogram bar. This (geometric) criterion can be written down as follows, according to [10,11]: the two nodes (words), e.g., $B_3(n)$ and $C_7(m=n+5)$, are connected if (see fig. 1)

$$\sigma_n, \sigma_m > \sigma_p$$
, for all $n . (2)$



Figure 1. An example of HVG construction

The process of constructing can be algorithmized. For example, in figure 1 the word node $A_1(n+2)$ is considered incident (and is connected with edges) to the words $B_3(n)$ and $C_1(n+5)$, $B_3(n)$ being the closest word to the left of $A_1(n+2)$ with a standard deviation estimate $\sigma_n = \sigma_B$ greater than that of the word A: $\sigma_{n+2} = \sigma_A$, and $C_7(m=n+5)$ being the closest word to the right of $A_1(n+2)$, for which $\sigma_m > \sigma_A$.

At the second stage, the derived network is compactified. All the nodes corresponding to a single word, e.g., the word A, are combined into a single node (naturally, occurrence numbers and positions of the words are lost). The connections of theses nodes are also combined. Note that there is no more than one edge left between any pair of nodes, multiple connections are removed (see fig. 2).

This means, in particular, that the degree (number of connections) of the node *A* does not exceed the sum of degrees $\sum_{k} A_{k}(n)$. As a result, the new network of words – *compactified horizontal visibility graph* (CHVG) – is constructed (fig. 2).



Figure 2. Two stages in construction of CHVG

Texts used for CHVG construction were the novels "The Master and Margarita" (original version) by Mikhail Bulgakov and "Moby-Dick; or, The Whale" by Herman Melville, as well as arrays of news information from the Web.

For all CHVG networks of words described here, the degree distribution is close to power law (fig. 3), i.e., these networks are scale free.

For comparison, was studied for the simplest language networks, where during the first stage of the network construction adjacent words were connected, and, at the second stage, the network was compactified. It is obvious that the weight of a node in such network corresponds to the word frequency, and the distribution of these weights follows the Zipf law [18]. The most connected are the nodes corresponding to the most frequently occurring words – conjunctions, prepositions, etc., which are very important for the text coherence, but are of little interest for the aspect of informational structure.



Figure 3. Node degree distribution (log-log scale) of CHVG constructed from "The Master and Margarita" (a) and "Moby-Dick; or, The Whale" (b). Horizontal axis contains node degrees k, vertical axis shows the values 1 - F(k), where F(k) is a distribution function of node degrees

Among the nodes with largest degrees, alongside with personal pronouns and other function words (particles, prepositions, conjunctions, etc.), are the words, which determine the informational structure of the text [16, 17].

Let Ψ be a set of *N* different words (in our case N = 100) corresponding to the largest-weight nodes of the aforementioned simple language network, and let Λ be a set of words corresponding to the largest-weight nodes of the CHVG. Then the set $\Omega = \Lambda \setminus \Psi$ will contain informational words, which are also important for the text coherence. Appendix gives juxtaposition of the top 100 largest-weight nodes for the two types of language networks constructed from the novels "The Master and Margarita" by Michael Bulgakov and "Moby-Dick; or, The Whale" by Herman Melville.

In particular, the Ω set of the CHVG built from "Мастер и Маргарита" contains such words as Иван, Мастер, Варенуха, Берлиоз, Бегемот, Римский, профессор, Левий, Иешуа.

The following results were obtained from studying the language networks:

- 1. An algorithm compactified horizontal visibility graph (CHVG) was proposed.
- 2. Language networks were built from different texts based on series of standard deviation estimates and CHVG.

3. In CHVG obtained from literary works, among the largest-degree nodes there are words responsible not only for the coherence of the text, but also for its informational structure. They reflect the meaning of the mentioned texts.

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Appendix

Table 1. Juxtaposition of the top 100 largest-weight nodes of the word networks constructed from Bulgakov's "The Master and Margarita"*

Simple network		CHVG]	Simple network		CHVG	
Weight	Word	Weight	Word	1	Weight	Word	Weight	Word
5724	И	14724	И	1	237	ЭТОТ	1020	ЧЕЛОВЕК
3591	В	12880	В	1	222	КОТ	1007	BAC
2235	HA	8069	HE	1	219	ПРОКУРАТОР	978	СКАЗАЛ
1893	HE	7550	НА		219	ГЛАЗА	961	ЭТОГО
1616	С	6511	ЧТО		215	СО	944	ГОСТЬ
1396	ЧТО	6050	OH		213	BAC	919	ГЛЕ
1204	OH	5225	ТО		212	ИЛИ	905	ВАРЕНУХА
1081	A	5224	Я		210	BOT	886	MACTEP
979	ЕГО	5105	С		209	СОВЕРШЕННО	871	НИКАНОР
936	ТО	4518	МАРГАРИТА		207	ЧЕЛОВЕК	866	БУФЕТЧИК
936	KAK	3642	ЕГО		206	ЛИ	861	УЖЕ
899	НО	3396	A		206	КОРОВЬЕВ	825	ТЕПЕРЬ
809	K	3009	K		204	ТЕПЕРЬ	815	EIIIE
760	Я	2996	KAK		199	ΑЗΑЗΕΛΛΟ	807	ЧТОБЫ
709	ИЗ	2848	ИВАН		197	ИХ	805	ИВАНОВИЧ
680	ПО	2847	ОНА		193	СКАЗАЛ	803	HV
634	3A	2562	ИЗ		187	НАЛ	798	СТЕПА
555	OT	2509	RЫ	-	184	BAM	790	НАЛ
553	V	2441	ΠΡΟΚΥΡΑΤΟΡ		183	СЕБЯ	766	BAM
534	OTC.	2317	3A	-	183	ОНИ	761	BO
521	BCE	2313	ПО		183	KTO	740	<u>римский</u>
520	WE.	2010	БЫЛО		182	БЫЛА	738	ОЧЕНЬ
514	OHA	2076	EDDINO EDDINO		177	ПЕРЕЛ	724	ОТВЕТИА
484	МАРГАРИТА	2057	НО		175	ТОТ	722	CO
460	EE	2000	v		172	YEPE3	720	КОГЛА
409	БЫЛО	1989	0		171	БЫЛИ	719	НИЧЕГО
403	ПОЛ	1940	EE	1	166	BO	671	МАРГАРИТЕ
403	БЫЛ	1914	BCE		165	ВОЛАНЛ	663	ΛΗΠΟ
400	ТАК	1904	KOPOBLEB		165	НЕГО	657	ПРОФЕССОР
382	ВЫ	1859	ВОЛАНЛ		162	ТОГЛА	656	ЛИ
379	УЖЕ	1815	БЫ		157	ОТВЕТИЛ	652	ИВАНА
375	ЕМУ	1761	БЫЛ		157	ΛΗΙΟ	651	ЧЕРЕЗ
333	БЫ	1721	KOT		156	ЛАЖЕ	649	МЫ
328	0	1696	ТАК		153	ВРЕМЯ	644	ВРЕМЯ
321	ТУТ	1693	ΑЗΑЗΕΛΛΟ		150	СЕЙЧАС	641	ДО
313	ТОЛЬКО	1687	ЖЕ		149	ЧЕМ	636	они
307	ЕЩЕ	1602	ПОД	1	149	ПИЛАТ	633	НЕГО
297	ТЫ	1568	ТЫ		147	ПРИ	623	ЭТОТ
297	MHE	1439	ПИЛАТ		147	ΠΟCΛΕ	619	ΠΟCΛΕ
281	НИ	1418	ОТ		147	ЕЙ	612	МАРГАРИТЫ
281	МЕНЯ	1374	БЕРЛИОЗ		145	ОПЯТЬ	609	БЕГЕМОТ
281	ЛА	1337	ни		144	НУ	607	ИХ
277	ЭТОГО	1323	MHE	1	141	КАКОЙ	598	ЧЕМ
276	ИВАН	1321	МЕНЯ	1	139	ЗДЕСЬ	590	ЕЙ
258	ГДЕ	1315	ЕМУ	1	139	МЫ	588	ТОГО
254	ЧТОБЫ	1208	ДА	1	138	НИЧЕГО	577	ЛЕВИЙ
254	ОЧЕНЬ	1179	ТУТ	1	138	КОНЕЧНО	575	СЕБЯ
250	КОГДА	1147	BOT	1	137	TAM	575	АФРАНИЙ
250	ДО	1095	HET	1	137	БЕЗ	569	ИЕШУА
241	HET	1030	ТОЛЬКО	1	136	ТОГО	568	КАКОЙ

* The words present in the first one hundred of CHVG nodes but absent from the first one hundred of simple network nodes are in bold. The most informationally significant words from the CHVG top 100, which are also present in simple network top 100, are in italics.

Simple	network	CHVG			
Weight	Word	Weight	Word		
6612	THE	41291	THE		
5589	AND	23567	OF		
4257	OF	17704	Ι		
3083	A	16585	A		
2862	ТО	16577	AND		
2730	IN	14853	HIS		
2050	ТНАТ	11976	IS		
1915	HIS	11961	TO		
1568	BUT	11582	HE		
1524	IT	11431	WAS		
1400	HE	10956	IN		
1341	WITH	9883	WHALE		
1301	FOR	9516	THAT		
1001	I	0244			
1201		7483			
1166	19	700/	VOU		
1150	WAS	6640			
11/2	THIS	6457	HIM		
1096		5707			
1000	DV	1967	DV		
077		4007			
911	30 OD	4733			
924	OR	4/4/	ALL		
007	AI	4047	WIIH		
847	FROM	4578	ME		
832	UN NOW	4511	BUI		
796	NOW	4403	HAD		
784	NOT	4182	YE		
733	WERE	4147	THEIR		
721	THERE	4143	FROM		
713	ONE	4038	FOR		
703	HIM	3921	MY		
697	THEIR	3645	WERE		
694	YOU	3618	NOT		
684	BE	3405	AT		
671	LIKE	3352	BOAT		
653	THEY	3289	SHIP		
643	THEN	3276	ON		
614	ARE	3238	ARE		
609	MY	3113	THEY		
597	HAD	3104	OR		
596	WHICH	3077	STUBB		
594	WHALE	3077	QUEEQUEG		
581	SOME	3052	NOW		
580	AN	3022	THERE		
563	NO	2997	CAPTAIN		
547	WHEN	2979	WE		
511	UPON	2869	SO		
502	HAVE	2635	WHICH		
479	ME	2618	SEA		
478	WHAT	2592	HER		

0:	1		0111/0
Simple net	WOIK	TT 7 - 1 - 1 - 4	CHVG
weight v	vora	weight	word
467 MO	T T	2591	SPERM
458 UU	1	2590	
451 WE	,	2575	HAVE
445 UP	YO .	2538	ULD THOU
441 IN1		2482	THOU
433 TH	ESE	2351	THEM
431 OL		2317	WHALES
429 AH	AB	2291	UNE
425 TH	EM	2259	IIS
425 115		2252	MAN
414 YE		2214	WHAT
397 YE	ľ	2187	STARBUCK
381 HE	R	2159	LIKE
380 WH	0	2085	WHITE
369 OV	ER	2053	INTO
361 STI	LL	2010	MORE
360 TH	OUGH	1981	NO
360 ON	LY	1944	THEN
353 MA	N	1934	SOME
352 HE	RE	1903	UP
351 WII	L	1891	AN
348 SEA	A	1872	UPON
343 SU	СН	1846	THESE
343 LOI	NG	1836	SUCH
339 VE	RY	1788	WHEN
338 WO	ULD	1694	BEEN
336 AB	OUT	1665	PEQUOD
331 TH	OSE	1634	ABOUT
326 BE	EN	1592	THOUGH
321 OT	HER	1589	SEEMED
320 YO	UR	1574	YOUR
318 TH	OU	1549	OVER
317 IF		1544	OUR
316 DO	WN	1540	THOSE
310 AN	Y	1540	DECK
307 AF1	ΓER	1521	HAS
306 MO	ST	1496	HEAD
304 SH	ΙP	1491	MEN
303 TW	0	1459	MOST
301 TH	AN	1446	WILL
301 CH	APTER	1443	WOULD
300 BE	FORE	1428	DOWN
295 GR	EAT	1419	DO
294 AG	AIN	1415	US
283 SEI	EMED	1415	HERE
283 BEI	ING	1300	GREAT
280 HO	W	1385	VET
270 WH	ILE	1357	SAID
275 CAI	PTAIN	1342	VERY
268 STI	IBB	1335	ANY

Table 2. Juxtaposition of the top 100 largest-weight nodes of the word networks constructed from Melville's "Moby-Dick; or, The Whale"*

* The words present in the first one hundred of CHVG nodes but absent from the first one hundred of simple network nodes are in bold. The most informationally significant words from the CHVG top 100, which are also present in simple network top 100, are in italics.